and then allowed to stand until darkened in a closed flask, which indicates a hydride transfer mechanism for this decomposition.

Our studies in this area are continuing with the investigation of solid state spectra, determination
of association constants and examination of the charge-transfer spectra of substituted tropenium halides.

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[Contributios from the Department of Chemistry of the University of California at Los Angeles, Calif.]

# Molecular Geometry. <br> II. Methyl-cyclohexanes and Cycloheptanes ${ }^{1,2}$ 

By James B. Hendrickson ${ }^{3}$

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Machine computation is applied to the calculation of the energy difference between axial and equatorial methyls on cyclohexane. A value of $1.01 \mathrm{kcal} /$ mole is obtained. Similar calculations for methyl groups on various discrete conformations of the flexible cycloheptane ring are also calculated and the use of these values in delineating the conformational analysis of substituted cycloheptanes is discussed.

The energy difference between axial and equatorial substituents on cyclohexane has long been a central feature of conformational analysis. The values generally accepted for this difference vary from $1.6-2.0 \mathrm{kcal} . / \mathrm{mole}$ for axial vs. equatorial methyl groups, derived from spectroscopic and thermodynamic considerations. ${ }^{4}$ The problem of calculating the energy difference ${ }^{2}$ between axial and equatorial methylcyclohexane seemed to be an important one for several reasons. Firstly, since this energy difference is made up mostly of a large number of fairly minor non-bonded interactions between the differently placed methyls and the ring, it provides an especially delicate test of the efficacy of a computer approach as well as of the accuracy of the $110 n-b o n d e d$ interaction functions chosen. Secondly, of course, the computed results may be compared with reliable experimental values, and, finally, should the computer technique provide a reasonable approxin1ation to the empirical values it ninight be used with some confidence to afford as well the corresponding energies of methyls on more coniplex rings. The latter is of particular importance in providing a semi-quantitative basis for conformational analysis in the conformationally more complex cycloheptane system.

Dissection of the problen11 for 111achine computation (see Fig. 1) involves assignment of a specific conformation to the ring and calculation of the total energy of the molecule with the methyl group attached at a given carbon, first in one orientation ( $\sigma$. axial) and then in the other ( $\sigma f$. equatorial); subtraction then affords the desired energy difierence. The choice of functions here follows the discussion in part I*; energy terns were considered to be those arising from bond angle bending, torsional strain around single bonds and non-bonded interactions between hydrogens; these are separately calculated, using the functions discussed in
(1) This work was supported in part by a generous grant from the National Institutes of Health.
(2) Paper I of the series: J. B. Hendrickson, J. Am. Chem. Soc., 83, 4537 (1961).
(3) Alfred P. Sloan Foundation Fellow
(4) W. C. Dauben and K. S. Pitzer, Chapp. 1 of 'Steric liffects in Organic Chemistry," ed. M. S. Newman, John Wilcy and Sons, 1ne, Now York, N. Y., $19 \overline{6} ;$ C. W. Beckett, K. S. Pitzer and R. Spitzer, J. Am. Chem. Soc., 69, 2488 (1947).
part $\mathrm{I},{ }^{2}$ and added to provide the total strain energy of the molecule. The energy so calculated is more or less meaningless in absolute terms, as it contains no assessment of bond or coulombic energies or of zero-point energies or terms for vibration and rotation of the various bonds. The exclusion of these terms is largely justified on the ground that they will cancel in any calculation of energy differences between closely related conformers. Nevertheless, such an approximation of second-order contributions probably puts a serious limitation on the accuracy of the values calculated. In any event the availability of empirical values for some of the energy differences so calculated can serve as a check on the validity of this approximation, as in the examples of part I. ${ }^{2}$

As the sum of the three energy ternns considered liere (angle bending, torsional strain and 11onbonded interactions of hydrogens) was already available from the previous computations ${ }^{2}$ for the parent ring itself, without added methyl, it was deemed simpler to start with this ring value and add to it the changes occasioned by attaching the methyl group. This involves adding the change in angle bending energy ${ }^{5}$ at the site of the new methyl, the torsional strain due to rotation ( $\omega_{\mathrm{M}}$ ) of the methyl group around its bond to the ring, and finally the sum of the new non-bonded $\mathrm{H}-\mathrm{H}$ interactions from the methyl hydrogens to the ring hydrogens and subtraction of those interactions due to that hydrogen replaced by the methyl group on the parent ring. The various $\mathrm{H}-\mathrm{H}$ distances to be calculated fron the methyl hydrogens $\mathrm{A}, \mathrm{B}$ and C are functions of the bond angles $\phi_{\mathrm{M}}, \theta_{n}$, $\theta_{3}$, etc., and of the dihedral (torsional) angles, $\omega_{\mathrm{M}}$, $\omega_{1}, \omega_{n}$, etc.; the latter are given as part of the definition of the parent ring and are modified for these distance calculations to substituents $\left(\mathrm{CH}_{3}\right.$ or $\mathrm{H})$ by addition or subtraction of the relevant projection angle, as $\mu_{\mathrm{M}}$, in Fig. 2.

In a general program for the computer, these interactions are all separately computed and added for each given parent ring conformation. Also, in
(5) The change in angle lomding strain at $C_{1}(\mathrm{Fig} .1)$ is computed b y adding the angle strain of the present attached grouns, i.c., 2lepal + $3 E \psi_{\mathrm{M}}$, and subtracting the angle strain dne to the two hydrogens on $C$ : in the parent ring (see Fig. 1, ref. 2).


Fig. 1.-Geometry of methyl on a general $\mathrm{C}_{n}$-ring. The rotation $\omega_{M}$ of the methyl group is defined, counterclockwise, from an $\omega_{M}=0^{\circ}$ position defined with $H_{A}$ antiparallel as shown above to $H_{1}$ :

$$
\tan \psi_{M}=\frac{2\left(\cos \phi_{M}-1\right)}{\sqrt{2\left(\cos \theta_{1}+1\right)-4 \cos ^{2} \phi_{M}}}
$$

order to search further for a minimum-energy conformation of the added methyl, both $\phi_{M}$ and $\omega_{M}$ are varied independently as well; variation of $\phi_{M}$ represents a tilting of the appended methyl from the tetrahedral while $\omega_{\mathrm{M}}$ represents rotation of the methyl, which will presumably be at minimum torsional strain with $H_{\mathrm{A}}$ antiparallel to $H_{1}\left(\omega_{\mathrm{M}}=\right.$ $0^{\circ}$ ) and will duplicate in configuration with each $120^{\circ}$ of rotation.

## Results

Methylcyclohexane.-When axial and equatorial methyl groups are compared on the simple chair cyclohexane (all bond angles tetrahedral, all $\omega_{i}=60^{\circ}$ ) the difference in energy between the two forms is calculated as $1.53 \mathrm{kcal} . /$ mole. Both equatorial and axial forms are found to be at a minimum with $\omega_{M}=0^{\circ}$, as expected. Furthernore, as expected, no alteration of the equatorial methyl from the simple cliair with $\phi_{M}=109.5^{\circ}$ and $\omega_{M}=$ $0^{\circ}$ gave a lower energy, so that the equatorial methyl is certainly most stable in this form. When the axial methyl is tilted somewhat, however, a considerable release of strain is provided, passing through a mininium at $\phi_{M}=112^{\circ}$ with $\Delta E=1.04$ kcal./mole and $\omega_{\mathrm{M}}=0^{\circ}$. Yet another mode of conformational variation is possible, however, by changing the entire cyclohexane ring. In the previous work ${ }^{2}$ a program was set up to define the cyclohexane geometry as the ring was progressively warped toward the transition shape between the chair and twist-boat, in which the dihedral at one bond is forced to $0^{\circ}$. An axial substituent on that bond will concomitantly be forced out into a more equatorial orientation and so free itself of nonbonded hydrogen interactions, although at the expense of increased angle strains in the ring itself. In the passage from $\omega_{1}=60^{\circ}$ to $\omega_{1}=0^{\circ}$, then, one may expect a conformation which balances these strains with a minimum of total energy. Accordingly, the same calculations, varying $\omega_{\mathrm{M}}$ and $\phi_{\mathrm{M}}$, were performed for each of the previously computed minimum-energy cyclohexane rings with successive values of $\omega_{1}$ decreasing from $60^{\circ}$. In this way an over-all minimum energy configuration was found


Fig. 2.-Projection down $\mathrm{C}_{1}-\mathrm{C}_{2}$ bond:

$$
\cos \mu_{\mathrm{M}}=\frac{\cos \phi_{\mathrm{M}}}{\sin \phi_{\mathrm{M}}}\left(\frac{1-\cos \theta_{\mathrm{J}}}{\sin \theta_{1}}\right)
$$

for the axial methylcyclohexane at $\omega_{1}=58^{\circ}, \phi_{\mathrm{M}}=$ $112^{\circ}$ and $\Delta E=1.01 \mathrm{kcal} . /$ mole. It will be seen that it is very similar to the minimum secured by simply bending the methyl group back on a normal cyclohexane. The energy difference is composed $66 \%$ of $\mathrm{H}-\mathrm{H}$ interactions in the latter case, however, whereas it is $78 \%$ in the former. Thus it may roughly be said that, using the present energy functions between a quarter and a third of the axial-equatorial methyl energy difference arises from angle and torsional strains, the rest from nonbonded interactions of hydrogens. The actual figure of $1.01 \mathrm{kcal} . /$ mole obtained is of course lower than the empirical value by a substantial proportion. On the other hand, when the uncertainty of the energy parameters is taken into account, the result may be accounted a satisfactory one.

Methylcycloheptane.-The same program used by the computer for computing the energy of a methyl group on a six-membered ring serves to compute that of the seven-membered ring cases as well. However, whereas in the methylcyclohexanes the basic chair ring conformation is clearly indicated by its unique position at the bottom of a potential energy well, the position of placement of a methyl on the seven-membered ring constitutes a much more complex problem. In the course of pseudorotation of the flexible chair cycloheptane, a given substituent, such as methyl, passes through a smoothly changing continuuni of conformational position or environnent and this may be characterized by a sequence of fifteen distinguishable conformational positions on the two symmetrical cycloheptane rings, clair $\left(\mathrm{C}_{\mathrm{S}}\right)$ and twist-chair $\left(\mathrm{C}_{2}\right)$, through which the pseudorotation passes. ${ }^{2}$ This sequence of fifteen conforn1ational positions on the two synnnetrical ring forms is the pseudorotation itinerary and consists of four axial and four equatorial positions in the chair cycloheptane and an axis-carbon ( $\mathrm{C}-1$ ) plus three axial and three equatorial positions on the twist-chair form. The two symmetrical cycloheptanes themselves are each characterized by four bond angles and four dihedral angles and it was found previously that the most stable conformations of these had bond angles somewhat larger than tetrahedral. ${ }^{2}$

If we consider the methylcycloheptane to be "frozen" in each one of these forms we can calculate for each separate position the energy of the added methyl on the ring as with cyclohexane above. For each such case we can further flex the ring angles and the angle at which the methyl is attached in order to find that particular molecular shape having the least energy. In the course of searching previously for the most stable parent cycloheptane ring we had examined the energies of a variety of

Table I
Energies of Methylcycloheptane Conformers

| Methyl position | $\Sigma E^{a}$ | $\Delta E{ }^{\text {b }}$ | $\phi_{\mathrm{M}}$ | $\omega_{\mathrm{M}}$ | Ring description ${ }^{\text {c }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Twist-chair ring |  |  |  |  |  |
| 1 (axis) | 10.65 | 0.03 | $\tau$ | $0^{\circ}$ | Normal |
| 2 e | 10.61 | $-0.01$ | $\tau$ | $0^{\circ}$ | Normal |
| 2 a | 14.92 | 4.27 | $114^{\circ}$ | $-4^{\circ}$ | $\theta=114^{\circ}$ |
| 3 e | 10.62 | 0.00 | $\tau$ | $0^{\circ}$ | Normal |
| 3 a | 15.50 | 4.88 | $114^{\circ}$ | $-26^{\circ}$ | $\theta=114^{\circ}$ |
| 4 e | 10.63 | 0.01 | $\tau$ | $0^{\circ}$ | Normal |
| 4 a | 12.05 | 1.43 | $112^{\circ}$ | $-14^{\circ}$ | Normal |
| Chair ring |  |  |  |  |  |
| 1 e | 12.77 | 2.15 | $\tau$ | $0^{\circ}$ | Normal |
| 1 a | 14.59 | 3.97 | $\tau$ | $0^{\circ}$ | $\theta=115^{\circ}$ |
| 2 e | 12.77 | 2.15 | $\tau$ | $0^{\circ}$ | Normal |
| 2 a | 14.41 | 3.79 | $112^{\circ}$ | $4^{\circ}$ | $\theta=113,111,116^{\circ}$ |
| 3 e | 12.77 | 2.15 | $\tau$ | $0^{\circ}$ | Normal |
| 3 a | 19.97 | 9.35 | $116.5^{\circ}$ | $36^{\circ}$ | $\theta=113,111,117^{\circ}$ |
| 4 e | 12.85 | 2.23 | $\tau$ | $0^{\circ}$ | Normal |
| 4 a | 13.64 | 3.02 | $110.5^{\circ}$ | $-10^{\circ}$ | Normal |

a $\Sigma E$ is the total calculated energy of ring with methyl attached and compensation for the replaced hydrogen at that carbon, in kcal./mole. $b \Delta E$ represents the difference from the average equatorial energy of $10.62 \mathrm{kcal} . / \mathrm{mole}$. ${ }^{c}$ The geometry of the rings is given below:

|  | $\theta_{1}$ | $\theta_{2}$ | $\theta_{3}$ | $\theta 4$ | $\omega_{1}$ | $\omega_{1}$ | $\omega *$ | $\omega^{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Twist-chair: Normal | $112^{\circ}$ | $112^{\circ}$ | $112^{\circ}$ | $112^{\circ}$ | $-41.2{ }^{\circ}$ | $97.0^{\circ}$ | $-75.8^{\circ}$ | $52.9{ }^{\circ}$ |
| $\theta=114^{\circ}$ | 114 | 114 | 114 | 114 | -39.7 | 91.7 | -72.2 | 50.8 |
| Chair: Normal | $\tau$ | 112 | 111 | 116 | 69.9 | $-91.8$ | 70.6 | 0.0 |
| $\theta=115^{\circ}$ | 115 | 115 | 115 | 115 | 55.3 | -86.0 | 71.7 | 0.0 |
| $\theta=113,111,116^{\circ}$ | $\tau$ | 113 | 111 | 116 | 68.2 | -91.4 | 70.6 | 0.0 |
| $\theta=113,111,117^{\circ}$ | $\tau$ | 113 | 111 | 117 | 70.0 | -90.2 | 68.8 | 0.0 |

rings with various bond angles ${ }^{6}$ so that these were available for calculation of the effect of substituting one methyl group by the above computer program, varying independently in each case the bond angle $\phi_{\mathrm{M}}$ of attachment of that methyl and its dihedral angle $\omega_{\mathrm{M}}$ of rotation around the $\mathrm{C}-\mathrm{CH}_{3}$ bond. For each case, the choice of parent rings used ${ }^{6}$ did in fact afford an energy minimum for the methyl. The values obtained are summarized in Table I.

To illustrate the procedure in more detail let us examine the calculation of the 2 -axial methyl on the twist-chair cycloheptane. A set of angles representing one parent ring is selected; the program then computes the energy of adding methyl at a bond angle $\phi_{\mathrm{m}}$ and rotating it in increments of $\Delta \omega_{M}$ through $120^{\circ}$. This yields a minimum at some orientation, $\omega_{M}$, of the methyl group attached at an angle $\phi_{M}$ to the ring. The procedure is repeated for values of $\phi_{\mathrm{M}} \mathrm{in}$ creasing from $\tau$ until the balance of the strain of enlarging $\phi_{\mathrm{M}}$ and the release of $\mathrm{H}-\mathrm{H}$ interaction energy affords a minimum energy for a methyl group in the 2 -axial position on one particular parent cycloheptane ring. In the case of the ring with all bond angles equal to $112^{\circ}$ (the preferred parent ring ${ }^{2}$ ), $\Sigma E=25 \mathrm{kcal} . /$ mole at $\phi \mathrm{m}=\tau$ and drops to a minimum of 15.8 kcal , at $\phi_{\mathrm{M}}=116.5^{\circ}$, i.e., as the methyl is bent back away from the compressed axial environment. Similar variations of $\Sigma E$ with $\phi_{M}$ and $\omega_{M}$ can be found for each of the parent rings available ${ }^{6}$ and from the whole set the conformation and energy of the particular 2 -axial-methyl twist-chain cycloheptane of lowest energy can be located. In this case the parent ring with all bond angles $114^{\circ}$ afforded the lowest $\Sigma E$ vs. $\phi \mathrm{m}$ minimum at $14.92 \mathrm{kcal} . /$ mole and $\phi_{M}=114.0^{\circ}$ (Table I). The parent rings with spread angles ${ }^{6}$ afforded no minima below 15.8 kcal . In every instance the minima were found at rotations, $\omega_{M}$, of the $2-$ axial methyl group between $90^{\circ}$ and $120^{\circ}\left(-30^{\circ}\right.$ and $\left.0^{\circ}\right)$.

In searching for minima, the rotation $\omega_{\mathrm{m}}$ occasionally exhibited two minimum-energy positions; the clearest example
(6) The cyclobeptanes used as parent rings for these methylsubstitution trials were both chair and twist-chair forms, either with all bond angles equal, from $109.5^{\circ}$ to $115^{\circ}$, or with a "spread" ring in which $C_{1}=109.5^{\circ}$ and $C_{2}, C_{3}$ and $C_{4}$ are varied independently from $109.5^{\circ}$ to $117^{\circ}$.
was the 1-axial-methyl in the chair conformation, for which the two minima always occurred at $\omega_{M}=0^{\circ}$ and $60^{\circ}$, positions which balance symmetrically the $\mathrm{H}-\mathrm{H}$ interactions of the methyl with the 3a-hydrogens, usually but not always with the lower minimum at $\omega_{M}=0^{\circ}$, i.e., with one methyl hydrogen in the mirror plane of the ring and between the two 3a-hydrogens. The latter position has more severe van der Waals repulsions but has the advantage of no torsional strain, whereas the conformation with $\omega_{m}=60^{\circ}$ has the methyl eclipsed but suffers least from $\mathrm{H}-\mathrm{H}$ repulsion. (Most of the preferred configurations of the methyl will be observed to be at or near $\omega_{M}=0^{\circ}$, the configuration with no torsional strain.)

Another effect of interest observed in the 1 -axial-methyl computations was that as the parent rings chosen afforded minima closer and closer to that of the best case, the value of $\phi_{\mathrm{M}}$ at the minimum decreased nearer to $\tau$, the value of $\phi_{\mathrm{n}}$ in the best case. This implies that in the successive chosen rings the 3 a-hydrogens are being spread farther apart until, in the best case, they are beyond reach of the 1-axial-methyl, which need not be tilted away from its axial position at all to avoid them. In the other cases, such ring spreading combined with this tilting ( $\phi_{\mathrm{M}}$ ) to produce the preferred orientation.
Increments of $2^{\circ}$ for $\omega_{M}$ and $0.5^{\circ}$ for $\phi_{\mathrm{M}}$ were finally used in obtaining the minimum energies and the latter are given to two decimal places, not to imply a useful accuracy of this degree but to show how closely the various equatorial methyls on different positions of one ring come to being equal in these computations. Since it would certainly be expected that they should be equal it is heartening to find this to be the case.

The data of Table I can now be applied to tracing an energy contour of the pseudorotation, as shown in Fig. 3. The curve follows the strain energy encountered by the methyl group as it passes through the pseudorotation itinerary, plotted as the abscissa. A number of interesting features emerge from examination of these data: 1. The calculations show that all the equatorial positions on one ring conformation prefer $\phi_{M}=\tau$ and have the same energy; also, as would be expected, the ring form for mini-


Fig. 3.-Pseudorotation of methylcycloheptane.
mum energy is the same with an equatorial methyl as it is for the minimum-energy parent cycloheptane ring itself. The energy of the equatorial-methyl-cycloheptanes is lower by $0.5 \mathrm{kcal} . /$ mole than that calculated for the ring itself (chair, 13.30; twist-chair, $11.14 \mathrm{kcal} .^{2}$ ), reflecting the net increase in dispersion or attractive interactions ( $\mathrm{H}-\mathrm{H}$ distances $\gtrsim 2.2 \AA$.) when the methyl is attached to the ring. Methyl-cycloheptane should be expected to partition among the twist-chair forms with equatorial methyls, these forms being freely interconvertible through pseudorotation.
2. The axis-carbon ( $\mathrm{C}-1$ ) of the twist-chair has two equivalent substituent positions, unlike any of the other carbons of cycloheptane (or cyclohexane); inasmuch as these previously have been considered to be intermediate in energy between axial and equatorial, ${ }^{2}$ it is important to note that the calculated energy of these positions is in fact virtually the same as that of the equatorial positions. This has the important consequence that a gem-dimethyl cycloheptane (and, by a reasonable extension, any 1,1-disubstituted cycloheptane) will take up preferentially the single conformation of a twist-chair with the two methyls on the axis-carbon; the preference for this form should be $1.4 \mathrm{kcal} . /$ mole, this being the energy difference between the axial and equatorial methyls on the next best position (twistchair, $4 \mathrm{e}-4 \mathrm{a}$ ) and hence the energy difference between 1,1-dimethyl- and 4,4-dimethyl-cycloheptanes (twist-chair). A comparable situation does not, of course, exist in cyclohexane cases.
3. The higher relative energy values for axial positions in methylcycloheptanes over methylcyclohexane is part of a trend from the slight distinction between axial and equatorial orientations in the many minimum-energy cyclopentane conformations ${ }^{2,7}$ to the very severe interactions which exist on "inside" positions of the medium ( $\mathrm{C}_{8-12}$ ) rings, ${ }^{8}$ where even the hydrogens are sterically, crowded so that the relative energies of "axial", methyls at those positions would be enormous. ${ }^{9}$ The highest axial energy in the cycloheptanes is that of the chair 3a-methyl ( $9.35 \mathrm{kcal} . /$ mole) and represents the height of the barrier to free pseudorotation among all the methylcycloheptane conformations.

[^0]

Fig. 4.-Equatorial positions on eycloheptane (twist-chair form; axialmethyl energies in parentheses).

Since it is less than the barrier to chair-boat interconversion in cyclohexane, ${ }^{2,10}$ we may assume that a rapid, thermal pseudorotation occurs in methylcycloheptane at ordinary temperatures. Although the calculated value for axial methylcyclohexane above is actually lower than the empirical value, it does not necessarily follow that the axial methylcycloheptane values given in the table are similarly low since many of the involved van der Waals interactions will be computed from different regions of the curve of $E=f(r)$, which may indeed vary in accuracy.
4. The values of $\Delta E$ in Table I are somewhat high since they all were calculated assuming only variations of ring shape which retained plane or axial symmetry in the parent cycloheptane ring. However, they should be essentially comparable to the $1.04 \mathrm{kcal} . /$ mole difference calculated in the cyclohexane case in which the chair symmetry was retained for the ring. Since this is very close to the $1.01 \mathrm{kcal} . /$ mole figure obtained by also warping the ring out of symmetry, the present figures for cycloheptane probably would be little changed by slight warping actions of this kind.

Figure 4 summarizes the inore stable twist-chair cycloheptane, showing the $\Delta E$ of axial-methyl substituents for each position as well as the approximate bond and dihedral angles (these vary slightly with the substituent; see Table I). At each position the equatorial bond is shown, alternately above and below the molecular plane as in chair cyclohexane; both positions at the axis-carbon are equatorial. This diagram is useful for assigning the preferred conformations of polymethylcycloheptanes and will be valid for this purpose as long as the substituents are not both cis and axial, in which case repulsions between the substituents thenisclves became important.

In using the diagram one can see that in 1,2-transdimethylcycloheptane any pair of vicinal ring positions are suitable to provide trans di-equatorial sites and the compound itself should partition equally among these four discrete twist-chair conformations via pseudorotation. The 1,2-cis isomer, by contrast, can achieve a minimum energy only by taking up the twist-chair conformation with one methyl on the axis-carbont. In a similar manner it is possible to examine all the possible polymethylcycloheptanes, assigning preferred conformations and minimum energies to the isomers. A table of all the di- and tri-methylcycloheptanes is appended

[^1](Table II). The table suggests that all dimethylcycloheptanes will have essentially the same energy, equal minimum-energy conformations being available for all, whereas four of the thirteen possible trimethyl isomers should be of higher energy than the rest by about $1.4 \mathrm{kcal} . /$ mole. The only relevant cycloheptanes studied to date are the cis- and trans-3, $\overline{\bar{b}}$-dimethylcycloheptanones, which differ in energy by $0.8 \mathrm{kcal} . /$ mole $^{11}$ and suggest the presence of several conformations, but since the effects studied here are fairly delicate and strongly influenced by geometrical changes, the presence of a carbonyl group is very likely to vitiate conclusions drawn on the hydrocarbons, so that this case cannot be taken as a relevant test.

The presence on cycloheptanes of other substituents which, unlike carbonyls, retain the tetrahedral configuration of the ring carbon may reasonably be treated like the methyl groups above in conformational analysis. Application of Winstein's $A$-values ${ }^{12}$ for different substituents to the axial-methyl energies at different conformational positions should provide a first approximation to the conformations of such derivatives of cycloheptanes. Thus, for example, all-trans-1-hydroxy$3, \overline{0}$-dimethylcycloheptane should take up the conformation with the hydroxyl group at the 4 -axial position, since its steric interference is about half that of the methyl group, leaving the methyls to occupy equatorial positions at ( $1,3^{\prime} \mathrm{e}$ ) or ( $2 \mathrm{e}, 2^{\prime} \mathrm{e}$ ).
(11) N. L. Allinger, J. Am. Chem. Soc., 81, 232 (1959).
(12) S. Winstein and N. J. Holness, ibid., 77, 5;62 (1950).

Table II
Preferred Conformations of Di- and Tri-methyl cycloheftanes

| Isomer ${ }^{\text {a }}$ |  | Preferred conformations | $\underset{\text { kcal./'mole }}{\Delta E E,}$ |
| :---: | :---: | :---: | :---: |
| 1,2 | c | (1,2e) | 0 |
| 1,2 |  | (1,2e), (2e, 3e), (3e, 4e), (4e, ${ }^{\prime} \mathrm{e}$ ) | 0 |
| 1,3 |  | (1,3e), (2e, 4 e$),\left(3 \mathrm{e}, 4^{\prime} \mathrm{e}\right)$ | 0 |
| 1,3 | t | (1,3e), (2e.2'e) | 0 |
| 1,4 | c | (1,4e), (2e, $\left.3^{\prime} \mathrm{e}\right)$ | 0 |
| 1,4 |  | (1,4e), (2e, $\left.4^{\prime} \mathrm{e}\right),\left(3 \mathrm{e}, 3^{\prime} \mathrm{e}\right)$ | 0 |
| 1,2,3 | c, ${ }^{\text {c }}$ | (3,4a,4'e) | 1.4 |
| 1,2.3 | c,t | (1,2e,3e), (2'e, 1,2e) | 0 |
| 1,2,3 | $t, t$ | (1,2e, 3e), (2e, 3e,4e), (3e, $4 \mathrm{e}, 4^{\prime} \mathrm{e}$ ) | 0 |
| 1,2,4 | c, $\mathrm{c}^{\text {c }}$ | (1,2e,4e), (2e, 1, 3'e) | 0 |
| 1,2,4 | c,t | (1,2e, 4a), (3e,4a, $\left.3^{\prime} e\right),(4 e, 4 a, 2 e),(4 a, 3 e, 1)$ | 1.4 |
| 1,2,4 | t, c | $\begin{aligned} & (1,2 e, 4 e),(2 e, 3 e, 4 ' e),\left(3 e, 4 e, 3^{\prime} e\right),\left(4^{\prime} e, 4 e, 2 e\right), \\ & (4 e, 3 e, 1) \end{aligned}$ | 0 |
| 1,2,4 |  | (2e, 1, 3'e), (3e, 2e, 2'e), (4e, 3e, 1) | 0 |
| 1,25 |  | (1,2e, $\left.4^{\prime} \mathrm{a}\right),\left(4 e, 4^{\prime} \mathrm{a}, 1\right)$ | 1.4 |
| 1,2,5 |  | (1,2e, 4'e) | 0 |
| 1,2,5 | t, c | (1,2c,4'e), (2e, 3e, 3'e), (3e,4e, 2'e), (4e, 4'e, 1) | 0 |
| 1,3,5 | c, ${ }^{\text {c }}$ | (1,3e, 4'e), (2e,4e, $3^{\prime} \mathrm{e}$ ) | 0 |
| 1,3,5 |  | (3e, 1, $3^{\prime} \mathrm{e}$ ), ( $4 \mathrm{e}, 2 \mathrm{e}, 2^{\prime} \mathrm{e}$ ), ( $4 \mathrm{e}, 3^{\prime} \mathrm{e}, 1$ ) | 0 |
| 1,3,5 |  | (1,3e,4'a), (2'e, $2 \mathrm{e}, 4 \mathrm{a}$ ) | 1.4 |
| ${ }^{\circ}$ As an example of the isomer notation used, ' $1,2,5-\mathrm{c}, \mathrm{t}$ ' refers to 1,2-cis,2, $\overline{0}$-trans-trimethylcycloheptane. ${ }^{b}$ The energy difference from the relevant all-equatorial isomer. |  |  |  |
|  |  |  |  |

In a similar vein the conclusions derived herein should provide a valid basis for conformational analysis of a wide variety of cycloheptane derivatives.

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# The Mechanism of the Reaction of 2-Picoline N-Oxide with Acetic Anhydride ${ }^{1}$ 

By Shigeru Oae, Teijiro Kitao and Yoshinori Kitaoka<br>Received Janutary 31, 1962


#### Abstract

2-Picoline $\lambda$ - oxide was allowed to react with acetic anhydride of which all three oxygens were equally enriched by oxygen18, and the 2-acetoxymethylpyridire obtained was hydrolyzed to 2-pyridinemethanol. Oxygen-18 analyses of these two compounds revealed that both carbonyl and ether oxygens of 2 -acetoxymethylpyridine have a mean value of one enriched oxygen-18 and one natural oxygen. The additions of large amounts of solvent and of DPPH did not affect the yield of tile main product. These observations, together with earlier findings, were considered as suggesting that the reaction proceeds via a "free radical pair" in solvent cage.


The reaction of 2 -picoline N -oxide with acetic anhydride has been shown independently by several different laboratories ${ }^{2-4}$ to give 2 -acetoxy methylpyridine. The benzoylation of quinaldine N-oxide has also been shown to give 2-benzoxymethylquinoline. ${ }^{5}$ The mechanism suggested then for the rearrangement is shown below, and this has been generally accepted for this and related reactions. ${ }^{2,4-7}$

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[^0]:    (7) K. S. Pitzer and W. E. Donath, J, Am. Chem. Soc. 81, 3213 (1959).
    (8) V. Prelog, J. Chem. Soc., 420 (1950).
    (9) Needless to say, substituents on these medium-size, flexible rings avoid the "inside" positions through pseudorotation so that examples for empirical comparison are not easily found.

[^1]:    (10) F. R. Jensen, D. S. Noyce, C. F. Sederholm and A. J. Berlin, J. Am. Chem. Soc., 82, 1256 (1960).

[^2]:    (1) Paper I11 on "Rearrangements of Tertiary Amine Oxides." A preliminary report appeared in paper 1 of this series: $S$. Oae, T. Kitao and Y. Kitaoka, Chemistry \&o Industry, 515 (1961); paper II: S. Oae T. Fiknmoto and M. Yamagami, Bull. Chem. Soc., Japar. 34, 1873 (1961)
    (2) G. Kobayashi and S. Furukawa, Pharm. Bull. Japan. 1, 347 (1953).
    (3) V. Boekelheide and W. J. Linn, J. An. Chem Sor. 76, 1286 (1954).
    (f) O. H. Bullitt and J. T. Maynard. ibit. 76. 1370 (19.;t).
    (5) I. J. Pachter. ibid., 75, 3020 (195'3).

[^3]:    (6) J. A. Berson and T. Cohen, ibid., 77, 1281 (19.55).
    (7) E. Matsumira, Memoirs of the Institute for Arts and Sciences, Liniv. of Osaka, 1, 1 (1952).

